



CATMULL-CLARK SUBDIVISION SURFACES EXACT EVALUATION AT ARBITRARY PARAMETER VALUES

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Abstract

In this paper, we invalidate the conviction far and wide inside the PC designs local area that Catmull-Clark development surfaces can't be assessed straightforwardly without expressly partitioning. We show that the surface and everything its subordinates can be assessed as far as a bunch of eigenbasis capacities that rely just upon the development plan and we determine scientific articulations for these premise capacities. Specifically, on the customary piece of the control network where Catmull-Clark surfaces are bi-cubic B-splines, the eigenbasis is equivalent to the power premise. Likewise, our strategy is both simple to execute and productive. We have utilized our execution to figure out excellent arch plots of development surfaces. The cost of our assessment conspire is practically identical to that of a bi-cubic spline. Subsequently, our strategy permits numerous calculations created for parametric surfaces to be applied to Catmull-Clark region surfaces. This makes development surfaces a much more alluring instrument for freestyle surface display. Involving development as an essential crude for the development of arbitrary geography, smooth, freestyle surfaces is appealing for content bound for a show on gadgets with incredibly differing delivering performance. Development normally upholds the level of detail delivering what's more, remarkable pressure calculations. While the basic algorithms are adroitly straightforward carrying out the player is troublesome motors that accomplish ideal execution on present-day CPUs such as the Intel Pentium family. In this paper, we portray an original table-driven assessment methodology for development surfaces utilizing, as an illustration, the plan of Catmull and Clark. Store cognizant plan and abuse of SIMD directions permit us to accomplish almost 100 percent FPU usage in the inward circle and accomplish a composite exhibition of 1.2 lemon/cycle on the Intel PIII and 1.8 lemon/cycle on the Intel P4 including all memory moves. The calculation upholds tradeoffs between store size and memory transport use which we inspect. A library that carries out this motor is openly accessible to the creators.

Keywords: linear algebra, subdivision surfaces, eigenanalysis, surface evaluation, parametrizations, Catmull-Clark surface.

1. INTRODUCTION

Region surfaces have arisen as of late as a strong and valuable procedure in demonstrating freestyle surfaces. In any case, in spite of the fact that in principle region surfaces concede nearby parametrizations, there is a compelling conviction inside the PC illustrations local area that these parametrizations can't be assessed precisely for erratic boundary values. In this paper, we negate this conviction and give a non-iterative method that effectively assesses Catmull-Clark region surfaces and their subsidiaries up to any request. The expense of our strategy is similar to the assessment of a bi-cubic surfacespline. The fast and exact assessment of surface parametrizations is vital for some standard procedures on surfaces, for example, picking, delivering, and surface planning. Our assessment technique permits an enormous assemblage of helpful procedures from parametric surfaces to be transferred to development surfaces, making them much more alluring as a freestyle surface demonstrating device. Our assessment depends on strategies originally created to demonstrate perfection hypotheses for development plans [3, 5, 1, 4, 7, 6]. These verifications are developed by changing the region into its eigenspace. In its eigenspace, the region is identical to a straightforward scaling of every one of its eigenvectors by their eigenvalue. These strategies permit us as far as possible places and cutoff normals at the vertices of the lattice, for instance. A large portion of the verifications, notwithstanding, consider just a subset of the whole eigenspace and don't address the issue of assessing the surface all over. We, on the other hand, utilize the whole eigenspace to determine a productively assessed scientific type of the development surface all over the place, even in the neighborhood of uncommon vertices. Along these lines, we have expanded a hypothetical device into an exceptionally functional one. In this paper, we present an assessment plot for Catmull-Clark region surfaces [2]. In any case, our procedure isn't restricted to these surfaces. At the point when development on the standard part of the lattice concurs with a known parametric portrayal [7], our methodology ought to be material. We have chosen to introduce the procedure for the extraordinary instance of Catmull-Clark region surfaces to show a specific model completely worked out. In reality, we have executed a comparable procedure for Loop's three-sided region plot [5]. The subtleties of that plan have surrendered a paper on the CDROM Proceedings [8]. We accept that Catmull-Clark surfaces have numerous properties which make them alluring as a freestyle surface plan device. For instance, after one development step each face of the underlying lattice is a quadrilateral, and on the standard piece of the cross-section, the surface is comparable to a piecewise uniform B-spline. Likewise, calculations have been composed to fair these surfaces [4]. To characterize a parametrization, we present another arrangement of eigenbasis capacities. These capacities were first presented by Warren in a hypothetical setting for bends [9] and utilized in a more broad setting by Zorin [10]. In this paper, we show that the eigenbasis of the Catmull-Clark region plan can be figured scientifically. Likewise, interestingly we show that in the normal case the eigenbasis is equivalent to the power premise and that the eigenvectors then compare to the "difference in premise network" from the power premise to the bi-cubic B-spline premise. The eigenbasis presented in this paper can along these lines be considered speculation of the power premise at exceptional vertices. Since our eigenbasis capacities are insightful, the assessment of Catmull-Clark region surfaces can be communicated logically. As displayed in the outcomes segment of this paper, we have carried out our assessment plot and involved it in numerous reasonable applications. Specifically, we show interestingly high goal ebb and flow plots of Catmull-Clark surfaces unequivocally figured around the sporadic pieces of the lattice. The paper is coordinated as follows. Segment 2 is a short audit of the Catmull-Clark development conspire.

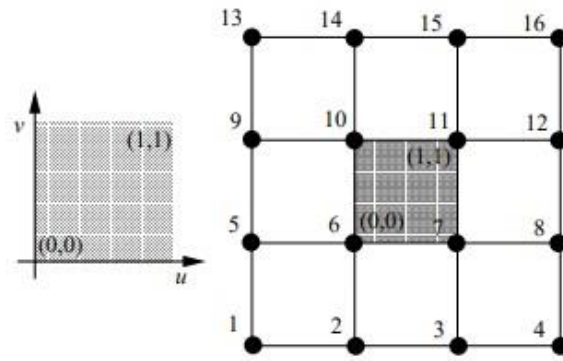


Fig 1: control vertices define a bi-cubic B-spline.

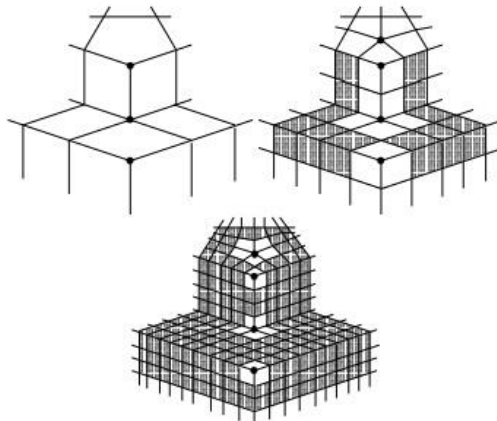


Fig 2: Two subdivision layers and an initial mesh

Added faces relate to standard bi-cubic B-spline patches. The dabs are unprecedented vertices. Segment 5 is a conversation about execution issues.

1.1 Notations

To make the inferences underneath as understood and minimal as potential we take on the accompanying notational shows. All vectors are thought to be sections and are indicated by boldface lower case roman characters, e.g., The parts of the vector are meant by the comparing emphasized character: the part of a vector is along these lines meant. The part of a vector shouldn't be mistaken for a filed vector. Lattices are meant by capitalized boldface characters. The translation of a vector is just a similar vector composed line-wise. Accordingly, the dab item between two vectors is composed. The vector or framework is meant to have just zero components. The size of this vector (lattice) ought to be clear from the setting.

2 CATMULL-CLARK SUBDIVISION SURFACES

The Catmull-Clark region conspire was created with the goal of displaying homogeneous control vertices on the base. The notable vertex of valence is Vertex 1. A smooth surface is defined by the right-hand side of Figure 2. The surface is defined as a cluster of growth phases that is restricted. The vertices of the cross-section are updated and new vertices are given at each step. This cycle is depicted in Figure 2. The valence of each vertex of the underlying lattice is the number of edges that meet at that vertex. An unprecedented vertex is one with a valence that is not equal to four. The lattice on the upper left-hand side of Figure 2 has two remarkable vertices of valence three and one of valence five. Away from remarkable vertices, the Catmull-Clark development is identical to midpoint uniform B-spline hitch inclusion. Thusly, the vertices encompassing a face that contains no phenomenal vertices are the control vertices of a uniform bi-cubic B-spline fix (shown schematically in Figure 1).

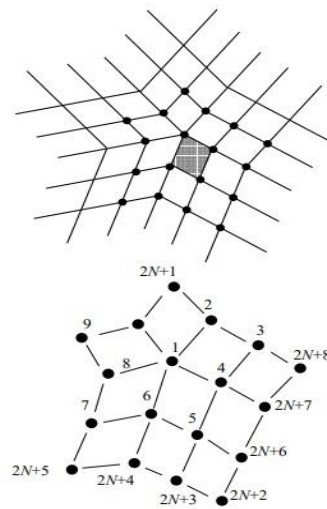


Fig 3: Surface patch near an extraordinary vertex with its control vertices. The ordering of the control vertices is shown on the bottom.

The countenances which relate to a standard fix are concealed in Figure 2. The figure shows how the piece of the surface containing normal patches develops with every region step. On a basic level, the surface can along these lines be assessed at whatever point the openings are adequately little to encompass the remarkable vertices. Tragically, this iterative methodology is too costly close to remarkable vertices, and doesn't give accurate higher subordinations. Since the control vertex structure close to an uncommon vertex is certifiably not a basic rectangular framework, all faces that contain phenomenal vertices can't be assessed as uniform B-splines. We expect to be that the underlying cross-section has been partitioned something like two times, secluding the exceptional vertices so that each face is a quadrilateral and contains at most one uncommon vertex. In the remainder of the paper, we want to show just how to assess a fix relating to a face with only one remarkable vertex, like the area close to vertex 1 in Figure 3. Allow us to signify the valence of that uncommon vertex. Our errand is then to track down a surface fix.

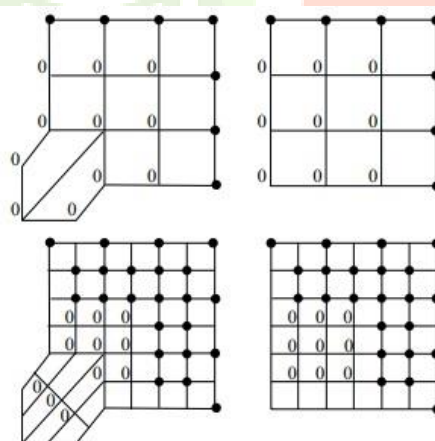


Fig 4: The valence of the remarkable vertex has no bearing on the action of the seven outer control vertices. The identical limit surface is achieved when the $2n+1$ control vertices in the center are set to zero.

2.1 Catmull-Clark Subdivision

The contribution to the region calculation is a control network, which should be a topological 2-complex conceivably with a limit (for nonmanifold region see [17]). This lattice might comprise appearances with inconsistent degrees (number of bounding edges) and vertices with inconsistent valence (number of occurrence faces). For effortlessness, we accept that all appearances of the cross-section are quads. In the event that this isn't true, one stage of standard Catmull-Clark development changes over an erratic

polygon network into one comprising of just quads. To permit wrinkles and corners, edges individually vertices can be labeled. Corners, which are inserted, might be arched or curved, the two cases requiring various standards. A vertex with one occurrence wrinkle edge is a "dart" vertex. A vertex with two episode wrinkles might be either a smooth wrinkle or a corner. A vertex with multiple-episode wrinkles should be a corner. At a corner, the wrinkles parcel the neighborhood of the labeled vertex into areas that can each be labeled as raised or curved. An area isn't affected by the geography or labels of another area, so while examining a corner vertex one just considers the two wrinkles which bound the area. Additionally, for wrinkle vertices, we might isolate the different sides of the wrinkle and treat them freely. Development continues by quadrisectioning each face and allocating direct situations toward every vertex in a better cross-section. These positions are midpoints of the point positions in the coarser lattice and are given in the type of stencils (see Figure 2). For additional subtleties on the standards and the thinking behind the loads, we allude to the peruser of the first paper by Biermann et al. [1]. Notice that all recently made vertices have valence four, i.e., they are normal. Therefore, later one development step all unique vertices are isolated by standard vertices and each face has all things considered one sporadic vertex, i.e., with a valence other than four. We exploit this in our execution to restrict the number of cases we really want to consider. The restriction of rehashed region yields the development surface.

2.2 Limit Surface Tessellation

Regularly just a limited number of development steps are performed, what's more, trailed by the utilization of the breaking point stencils. These are comparative to the ordinary development stencils yet convey loads that move the focuses in one last averaging step as far as the possible surface. For subtleties on limit stencils as well as a cutoff surface digression, stencils see [1]. Frequently few development steps are adequate for everything except the most bended models. For instance, one degree of the region to isolate all unpredictable vertices followed by five levels of extra region produces $(26)^2 = 4096$ quads for every unique face. The part of the cutoff surface compared to one face in the control network comprises a fix. Since the region rules take just prompt neighbors into account and rely just upon the neighborhood construction of the lattice, every unique control point impacts a limited part of the cutoff surface in its area. Specifically, for the guidelines of Biermann et al. (expecting $s = 1$ for every single inward corner; see Section 3), the control set of a fix is for the most part those vertices that have a place with the set of countenances offering an edge or vertex to the related control network face (see Figures 3 and 5). This suggests that each fix can be delivered free of any remaining patches if the 1-ring of neighbors of the related control network face is gathered up and passed to the suitable assessment schedule.

2.3 Basis Functions

On account of the linearity of the development interaction the last surface can be perceived as a straight mix of premise capacities with

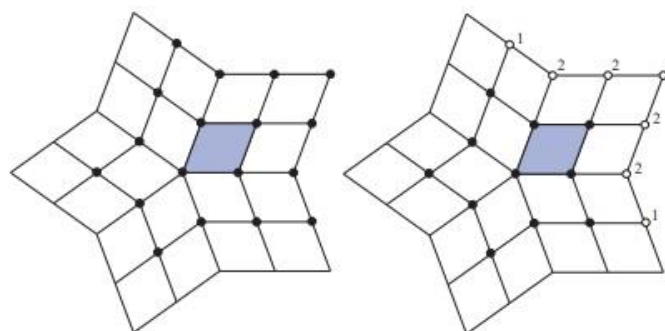


Fig 5: One of the incidents first-level faces of an inner irregular vertex of valence five are highlighted.

The black dots on the left represent the basis functions whose support spans the specified face. For all faces consequent to the irregular vertex, just one set of basis functions is required due to rotational symmetry. The control set is further divided on the right into the basis functions in the irregular vertex's 1-ring (black dots) and the outer seven bases (white dots). There are just two unique types of modulo symmetries (as shown by the designations "1" and "2").

$$s(u, v) = \sum_i B^i(u, v) p_i.$$

Here p_i is the control focuses, normally conveying (x, y, z) positions in world space, in spite of the fact that they frequently likewise convey surface directions, colors, and so forth. The B^i are the premise capacities, one focused at every vertex. The premise capacities are characterized as the consequence of partitioning a unit ball. For instance, build a control network in the x/z-plane what's more, move one control highlight $y = 1$ to deliver the related premise work. The last surface is hence a direct mix of such premise works each weighted by the real control point in the control network. The ordinary help of such a premise work is a 2-ring around the related vertex. The space for the boundaries (u, v) is the first control network, with every quad face defining its related breaking point fix for $(u, v) \in [0, 1]^2$. The cutoff fix decorations produce tests of the cutoff surfaces normally connected with dyadic places in the space. For instance, after d degrees of the region, the cutoff focuses on the decoration related to boundary values $(u_n, v_m) = (n/2^d, m/2^d)$, $n, m = 0, \dots, 2^d - 1$. The basic perception for our calculation is that the B^i depends just on the network of the cross-section and the presence of labels, yet not on the real control focuses. The last option just enters at runtime. Given some boundary values (u_n, v_m) related to a specific fix the example of the surface is found as

$$s(u_n, v_m) = \sum_i B^i(u_n, v_m) p_i.$$

The aggregate can be additionally confined to just those vertices whose premise capacities make a non-no commitment over the chosen fix, i.e., the 1-ring of the related control network face.

2.4 Algorithm Overview

The essential thought is to assess each cutoff fix consistently to a client chosen profundity straightforwardly from the control focuses utilizing precomputed clusters that contain uniform samplings of the premise capacities (premise work "tables"). In any case, the quantity of unmistakable premise capacities is unbounded since they depend, among different boundaries, on the vertex valences. In any event, when restricted by a most extreme vertex valence there is as yet a preposterously large number of premise capacities. The issue is additionally intensified while allowing wrinkles and corners on the surface. To work on this present circumstance, an underlying development step is performed utilizing the recursive standards, so that every first level quad has all things considered one unpredictable vertex (see Section 2.1). Thus, the premise capacities with help on a given fix are a capacity just of the valence of the one unpredictable vertex of that fix. Also, this first level of the region gives a potential chance to apply the digression space changes [1] fundamental for inward corners. The creation of the cutoff surface decoration continues one fix at a period. Since assessment of one fix affects the assessment of whatever other patches this should be possible in equal, however, we did not yet take advantage of this in our execution. For a given first-level quad, gather all control focuses in its 1-ring. Utilizing the premise work tables (see Section 2.2), produce a uniform decoration of this fix of the cutoff surface with each point in the decoration a weighted amount of control focuses, the loads being the comparing premise work inspected by then (see Section 2.3).

2.5 Algorithm Details

As the greatest number of development levels we picked five in expansion to the underlying recursive development venture, as this appears to be above and beyond for useful purposes. To assess a fix to profundity five requires the premise capacities to be assessed on a framework of $(25 + 1)(25 + 1) = 33 \times 33$ consistently divided example focuses. The tables are put away in memory as straightforward float[33*33] exhibits. To partition to less levels, just subsample these tables with a uniform lattice of size $(2d + 1)(2d + 1)$ where d is the quantity of levels. Pseudocode for the calculation (expecting five degrees of development) is as per the following:

```
// N = number of control focuses in 1-ring of face
// C = number of channels: x, y, z, s, t, r, g, b, and so forth.

float sample[C][33*33];

float bases[N][33*33];

float control[N][C];

for( k = 0; k < C; ++k )//circle over x,y,z

for( j = 0; j < N; ++j )

for( I = 0; I < 33*33; ++i )

sample[k][i] += bases[j][i]*control[j][k]
```

The above code just shows calculation of the surface examples.

On the off chance that digression vectors are wanted extra tables are expected for digressions in u and v parametric bearings. These future amassed utilizing the fitting channels of the control focuses. Ordinarily just (x, y, z) , a few applications may likewise require subsidiaries of different channels. Vectorization The deepest circle is effectively vectorized, by the same token physically or by a cutting edge compiler², to make the most of the Intel Streaming SIMD Extensions (SSE). Therefore we picked to make the circle over the directions of the peripheral circle all things considered the deepest. The circle through the tables vectorizes all the more proficiently and adding more arranges to the vertices is presently straightforward. Since there are eight XMM3 registers, the circle over the control focuses can be unrolled multiple times, involving four registers for premise work information and four registers for control point organizes. Utilizing this game plan of circles, control focuses can remain in registers all through the execution of the deepest circle. The four registers containing premise work information each contain four continuous passages from an alternate premise work table. The four registers containing control point information each contain a solitary direction of a control point rehashed multiple times. Control network faces at the principal level of the region are arranged in light of the valence of their (main) sporadic vertex, what's more, any labels, to guarantee that appearances with a similar premise capacity will be partitioned consecutively. Ideally, the premise work tables can remain in the L2 reserve between calls to the above work, really taking out any heap time for the tables. This additionally implies that speed ought to be generally autonomous of the intricacy of the lattice. That is, networks with various valence vertices and labels can be assessed at a generally similar rate as cross-sections with for the most part ordinary geography since tables will seldom be stacked from memory in either case. Trial results have affirmed this.

3 BASIS FUNCTION TABLE GENERATION

The premise capacities were precomputed by creating base cross-sections that remember just a single premise work for a specific direction and partitioning those base lattices utilizing a current recursive execution. Figure 4 shows a regular base lattice with the whole cross-section in the x/z -plane with the exception of one control point which has $y = 1$ on the left, what's more, the outcome after three degrees of development and cutoff stencil assessment on the right. The y -upsides of this fix are the premise work assessed on a 9×9 matrix.

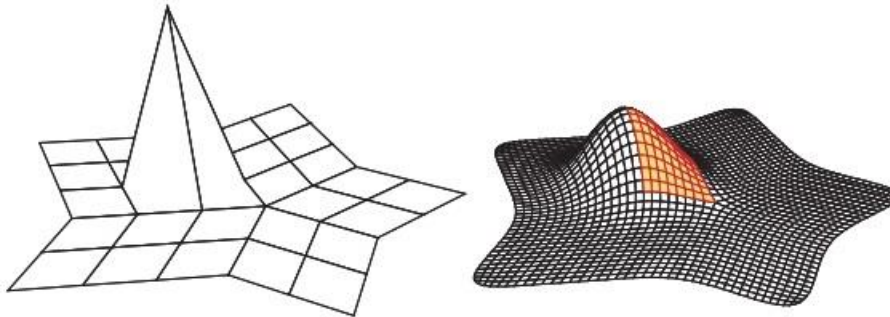


Fig 6: A base mesh (left) that was used to produce one of the basis functions for an irregular vertex with valence five, as well as the generated basis function level three evaluation, with the central patch marked (right). The basis function is evaluated at the y -values of this patch on a 9×9 grid.

Premise capacities were produced for valences 3-12 for inside focuses; 1-6 for wrinkle vertices and curved corners; 2-6 for sunken corners; and 3-7 for dart vertices⁴. For this large number of cases, limit positions and incomplete subordinates in the two parametric headings were tested on a 33×33 framework. To work on our code we didn't take benefit of the relative multitude of accessible balances. This brought about roughly 5300 tables absolute for values and subordinates. In applications in which the all-out table size must be kept tight, the quality of accessible balances can decrease the vital tables altogether. The tables were created with Subdivide 2.0 by Biermann and Zorin [1].

3.1 Counting Basis Functions

We presently go to a few itemized issues during table age. For motivations behind this conversation we generally have a recognized vertex. This is the single vertex in a given first level face which likewise exists in the base lattice. Overall this is a sporadic vertex, however, its valence might be four, making it as a matter of fact normal. We disregard this differentiation underneath and for effortlessness will constantly talk about the recognized vertex as the "unpredictable vertex." Smooth inside patches have control sets that comprise all the vertices in the 1-ring of the sporadic vertex as well as seven extra premise capacities not in the 1-ring (Figure 3). There is a line of balance on the askew of such a fix and of the seven premise capacities not in the vertex 1-ring, just two are unmistakable (named "1" furthermore "2" in Figure 3), and these are the equivalent paying little mind to valence, what's more, won't be counted here. For an unpredictable vertex of valence k , the quantity of particular premise capacities is $k + 2$. Dart, wrinkle, and corner patches are those for which the unpredictable vertex has one (dart) or two (wrinkle, arched corner, curved corner) episode labelled edges. For such fixes, the premise capacities are reliant upon the area of the fix concerning the tag(s). Figure 5 (top) shows an illustration of a dart vertex (base) and shows the course of action for a wrinkle or corner (raised or inward) vertex. There are $dk/2e$ particular patches because of evenness. Each particular fix has an unmistakable premise work for every vertex in the 1-ring of the sporadic vertex, in addition to one for the unpredictable vertex itself: $2k + 1$ for dart vertices, $2(k + 1)$ for wrinkle and corner (arched/inward) vertices. The absolute count of particular premise capacities at a labeled vertex with k episode faces is around $4(k + 1)2$. Outside the 1-ring are four extra premise capacities which are generally the equivalent no matter what the fix and label areas and valence. Two of these are equivalent to in the inside case

CONCLUSION

We have exhibited an incredibly productive way to deal with development in view of precomputed decorations of Catmull-Clark premise capacities. These can be delivered with any standard region code and may contain wrinkle, dart, and corner rules. The technique persists in other development approaches in a direct design. The calculation is appropriate for parallelization both at the level of SIMD tasks and at the degree of equal execution units. The outcomes ought to apply similarly well to other current CPUs with numerous execution units, profound pipelining, and their overall awareness of reserving issues. The upgrades in the memory design of the P4, specifically less transport move asset conflict inside the CPU and quicker admittance to the reserve, yield an exhibition improvement of the half. In future work, we desire to perform greater execution examinations between our table-driven approach and profundity first recursive region as well as forward distinction-based approaches. The recursive form is exceptionally compelling for multiresolution surfaces which add detail removals at each development level to essentially enhance the arrangement of surfaces that can be demonstrated in this design. Such a motor would likewise be extremely helpful for quick decompression of calculation [10]. Extra work ought to be given to versatile delivery measures which can be assessed quickly enough to amortize their expense

REFERENCES

- [1] BIERMANN, H., LEVIN, A., AND ZORIN, D. Piecewise Smooth Subdivision Surfaces with Normal Control. Proceedings of SIGGRAPH 2000 (2000), 113–120.
- [2] BISCHOFF, S., KOBELT, L. P., AND SEIDEL, H.-P. Towards Hardware Implementation Of Loop Subdivision. 2000 SIGGRAPH / Eurographics Workshop on Graphics Hardware (2000), 41–50.
- [3] BRICKHILL, D. Practical Implementation Techniques for Multi-Resolution Subdivision Surfaces. In Game Developers Conference, 2001.
- [4] CATMULL, E., AND CLARK, J. Recursively Generated B-Spline Surfaces on Arbitrary Topological Meshes. Computer Aided Design 10, 6 (1978), 350–355.
- [5] DEROSE, T., KASS, M., AND TRUONG, T. Subdivision Surfaces in Character Animation. Proceedings of SIGGRAPH 98 (1998), 85–94.
- [6] HAVEMANN, S. Interactive Rendering of Catmull/Clark Surfaces with Crease Edges. Tech. Rep. TUBSCG-2001-01, TU Braunschweig, 2001.
- [7] INTEL CORPORATION. C++ Class Libraries for SIMD Operations Reference Manual., 1997–1999.
- [8] INTEL CORPORATION. IA-32 Intel Architecture Software Developer’s Manual, 1997-2001.
- [9] JUNKINS, S. Fast Triangle Neighbor Finding for Subdivision Surfaces. Tech. rep., Intel Architecture Labs, September 1999.
- [10] KHODAKOVSKY, A., SCHRODER, P., AND SWELDENS, W. Progressive Geometry Compression. Proceedings of SIGGRAPH 00 (2000), 271–278.
- [11] LIEN, S.-L., SHANTZ, M., AND PRATT, V. Adaptive Forward Differencing for Rendering Curves and Surfaces. Computer Graphics (Proceedings of SIGGRAPH 87) 21, 4 (1987), 111–118.
- [12] LOOP, C. Smooth Subdivision Surfaces Based on Triangles. Master’s thesis, University of Utah, Department of Mathematics, 1987.
- [13] MULLER, K., AND HAVEMANN, S. Subdivision Surface Tessellation on the Fly using a versatile Mesh Data Structure. Computer Graphics Forum 19, 3 (2000).

- [14] PULLI, K., AND SEGAL, M. Fast Rendering of Subdivision Surfaces. In *Rendering Techniques '96*, 61–70, 1996.
- [15] SAMET, H. *The Design and Analysis of Spatial Data Structures*. AddisonWesley, 1990.
- [16] STAM, J. Exact Evaluation of Catmull-Clark Subdivision Surfaces at Arbitrary Parameter Values. *Proceedings of SIGGRAPH 98 (1998)*, 395–404.
- [17] YING, L., AND ZORIN, D. Nonmanifold Subdivision. In *Proceedings of Visualization 2001*, 2001.
- [18] ZORIN, D., AND KRISTJANSSON, D. Evaluation of Piecewise Smooth Subdivision Surfaces. *Visual Computer (2002)*.
- [19] ZORIN, D., AND SCHRODER , P., Eds. *Subdivision for Modeling and Animation. Course Notes*. ACM Siggraph, 2000.
- [20] ZORIN, D., SCHRODER , P., AND SWELDENS, W. Interactive Multiresolution Mesh Editing. *Proceedings of SIGGRAPH 97 (1997)*, 259–268.

