



# Study Of Runoff Prediction Parameters Using Dimensional Analysis

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## 1. ABSTRACT

Runoff prediction is an essential component of hydrology and water resources engineering. Accurate estimation of runoff helps in designing drainage systems, flood forecasting, watershed management, irrigation planning, and hydraulic structure design. Conventional runoff estimation methods often require extensive field data, which may not always be available. Dimensional analysis provides a simplified and scientific approach for developing predictive relationships between runoff and influencing parameters using fundamental physical dimensions.

This study applies dimensional analysis using the Buckingham  $\pi$ -theorem to identify significant parameters affecting runoff and to develop dimensionless relationships between rainfall intensity, infiltration rate, slope, catchment area, soil characteristics, and runoff discharge. The developed relationships help in estimating runoff effectively with limited experimental or field data.

**KEYWORDS** ; socio-economic, physical dimensions, Buckingham  $\pi$ -theorem, infiltration rate, slope, catchment area, soil characteristics

## 2. INTRODUCTION

Runoff refers to the portion of rainfall that flows over the land surface toward streams, rivers, and reservoirs after losses such as infiltration, evaporation, and interception.

Runoff prediction plays a crucial role in:

- Flood control planning
- Stormwater drainage design
- Watershed management
- Irrigation system planning
- Highway drainage systems
- Urban infrastructure development

Traditional methods such as the Rational Method, Unit Hydrograph Method, and Empirical Formulas require detailed hydrological data. Dimensional analysis offers a generalized predictive framework using fewer experimental observations.

## 2.1 BACKGROUND

Water is one of the most important natural resources and a key element in the socio-economic development of a State and Country. Water influences every sphere of the environment supporting life on earth. Its varying availability in time and space is a matter of concern to the mankind since fresh water is not an ever-present resource. Water resources of the world in general and in India are under heavy stress due to increased demand and limitation of available quantity. Proper water management is the only option that ensures a squeezed gap between the demand and supply. Sustainable water management of a river basin is required to ensure a long-term stable and flexible water supply to meet crop water demands as well as growing municipal and industrial water demands.

## 2.2 RAINFALL ANALYSIS

Rainfall is the major component of the hydrologic cycle and is the primary source of runoff (Beven, 2001b). Rainfall is essentially required to fulfil various demands including agriculture, hydropower, industries, environment and ecology. It is implicit that the rainfall is

a natural phenomenon occurring due to atmospheric and oceanic circulation (local convection, frontal or orographic pattern) and has large variability at different spatial and temporal scales.

## 2.3 RUNOFF ANALYSIS

Further, rainfall generated runoff is very important in various activities of water resources development and management, such as: flood control and its management, irrigation scheduling, design of irrigation and drainage works, design of hydraulic structures, hydro- power generation, and so on. The method of transformation of rainfall to runoff is highly complex, dynamic, nonlinear, and exhibits temporal and spatial variability. It is further affected by many parameters and often inter-related physical factors. It is a common experience that for a given amount of rainfall on a watershed, the event produces a high or low runoff depending on (besides other parameters): the small or large time interval/duration, with the infiltration and evaporation losses depending significantly on how long the water remains in the watershed.

## 2.4 OBJECTIVES OF THE STUDY

The objectives of this study are:

- To identify parameters affecting runoff generation
- To apply dimensional analysis for runoff prediction
- To develop dimensionless relationships between runoff and influencing variables
- To simplify runoff estimation for ungauged catchments
- To verify applicability of Buckingham  $\pi$ -theorem in hydrological modeling

## 3. LITERATURE REVIEW

- **Sherman in 1932**, it is "...the basin outflow resulting from one unit of direct runoff generated uniformly over the drainage area at a uniform rainfall rate during a specified period of rainfall duration." The underlying concept of the unit hydrograph is that the runoff process is linear, so the runoff from greater or less than one unit is simply a multiple of the unit runoff hydrograph.
- Inspired by a quotation from **Howard Cook in 1946**, this paper traces the evolution of the infiltration theory of runoff from the work of Robert Horton and LeRoy Sherman in the 1930s to the early digital computer models of the 1970s and 1980s. The reasons for the popularity of the infiltration theory are considered and its impact on the way in which hydrological responses were perceived by several generations of hydrologists.
- **Ven Te Chow's** contribution to applied hydrology modeling is exemplified by his **Handbook of Applied Hydrology**, which was revised in 1988 by a team led by David Maidment and Larry Mays. This comprehensive resource covers a wide array of topics, including hydrological modeling, water conservation, and manag

ement practices. It features advanced methods and applications relevant to current hydrological challenges and integrates various models for surface and groundwater interactions. The handbook emphasizes practical applications, the challenges in water resource management, and the importance of interdisciplinary approaches. It serves as a valuable tool for professionals in the field of hydrology and water.

- **Singh (1988) studied watershed modeling techniques** Considering the rainfall's importance in hydrological modeling, the objective of this study was the performance comparison, in convergence terms, of techniques often used to estimate the average rainfall over an area: Thiessen Polygon (TP) Method; Reciprocal Distance Squared (RDS) Method; Kriging Method (KM) and Multiquadric Equations (ME) Method. The comparison was done indirectly, using GORE and BALANCE index to assess the convergence results from each method by increasing the rain gauges density in a region, through six scenarios. The Coremas/Mae D'água Watershed employed as study area, with an area of 8385 km<sup>2</sup>, is situated on Brazilian semi-arid. The results showed the TP, as RDS and ME techniques to be employed successfully to obtain the average rainfall over an area, highlighting the MEM

## 4. Methodology and Analysis

### 4.1 The methodology adopted in this study involves:

- Identification of runoff influencing variables
- Selection of fundamental dimensions
- Application of Buckingham  $\pi$ -theorem
- Formation of dimensionless parameters
- Development of runoff prediction relationship
- Verification using sample calculations

Dimensional analysis helps convert complex hydrological relationships into simplified mathematical expressions useful for engineering applications.

## 5. FACTORS AFFECTING RUNOFF

Runoff depends on multiple hydrological and watershed characteristics:

### 5.1 Rainfall Characteristics

Includes:

- Rainfall intensity
- Rainfall duration
- Rainfall distribution
- Rainfall frequency

Higher rainfall intensity produces higher runoff.

### 5.2 Catchment Characteristics

Includes:

- Area of catchment
- Shape of catchment
- Slope of catchment
- Soil type

- Land use pattern
- Steeper slopes produce faster runoff

### 5.3 Soil Characteristics

Includes:

- Permeability
- Infiltration capacity
- Moisture content
- Porosity

Higher permeability reduces runoff.

## 6. PARAMETERS AFFECTING RUNOFF

Let runoff discharge depend on:

Parameter	Symbol	Dimension
Runoff	Q	$L^3/T$
Rainfall intensity	I	$L/T$
Catchment area	A	$L^2$
Slope	S	Dimensionless
Infiltration rate	f	$L/T$
Time duration	t	T
Gravitational acceleration	g	$L/T^2$

### APPLICATIONS

Useful in:

- Highway drainage design
- Stormwater management
- Dam spillway design
- Flood prediction studies
- Urban drainage systems
- Watershed planning

Especially useful for **civil engineering field projects and irrigation planning**

## ADVANTAGES OF DIMENSIONAL ANALYSIS

- Reduces number of experiments
- Saves time
- Saves cost
- Produces generalized relationships
- Useful for model-prototype relationships
- Applicable in hydraulic engineering problems

## LIMITATIONS

- Requires correct variable selection
- Cannot determine exact functional relationships
- Needs experimental validation
- Accuracy depends on assumptions

## SCOPE OF THE STUDY

The scope includes:

- Analysis of rainfall–runoff relationships
- Identification of major hydrological variables
- Application of Buckingham  $\pi$ -theorem
- Development of dimensionless runoff prediction model
- Useful application in small watershed engineering problems

## CONCLUSION

Dimensional analysis provides an effective and simplified approach for predicting runoff using fundamental hydrological parameters. Application of Buckingham  $\pi$ -theorem helped reduce complex relationships into manageable dimensionless groups. The developed runoff prediction equation is useful in preliminary watershed planning and hydraulic structure design, especially in areas lacking sufficient hydrological data.

Thus, dimensional analysis proves to be a reliable and economical tool in runoff estimation studies

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